The Lamb shift in muonic hydrogen


Abstract: The long quest for a measurement of the Lamb shift in muonic hydrogen is over. Last year we measured the energy splitting (Pohl et al., *Nature*, 466, 213 (2010)) in $\mu p$ with an experimental accuracy of 15 ppm, twice better than our proposed goal. Using current QED calculations of the fine, hyperfine, QED, and finite size contributions, we obtain a root-mean-square proton charge radius of $r_p = 0.841 84 (67)$ fm. This value is 10 times more precise, but 5 standard deviations smaller, than the 2006 CODATA value of $r_p$. The origin of this discrepancy is not known. Our measurement, together with precise measurements of the 1S–2S transition in regular hydrogen and deuterium, gives improved values of the Rydberg constant, $R_\infty = 10 973 731.568 160 (16) \text{ m}^{-1}$ and the rms charge radius of the deuteron $r_d = 2.128 09 (31)$ fm.

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Résumé : La longue quête d’une mesure du décalage de Lamb dans l’hydrogène muonique est terminée. L’an dernier, nous avons mesuré la séparation en énergie $2S_{1/2}^F=1–2P_{3/2}^F$ dans $\mu p$ (Pohl et al., *Nature*, 466, 213 (2010)) avec une précision expérimentale de 15 ppm, deux fois meilleure que notre objectif initial. Utilisant des calculs QED contemporains des contributions fines, hyperfines, QED et de dimension finie, nous obtenons une valeur quadratique moyenne du rayon de charge du proton égale à $r_p = 0.841 84 (67)$ fm. Cette valeur est 10 fois plus précise, mais 5 déviations standard moindre que la valeur CODATA 2006 pour $r_p$. L’origine de ce désaccord reste inconnue. Notre mesure, avec des mesures précises de la transition 1S–2S dans l’hydrogène et le deutérium ordinaires, donne de meilleures valeurs pour la constante de Rydberg, $R_\infty = 10 973 731,568 160 (16) \text{ m}^{-1}$ et pour le rayon de charge du deutéron $r_d = 2,128 09 (31)$ fm.

[Traduit par la Rédaction]
1. Introduction

The observation of Lamb and Retherford [1] that the 2S\(_{1/2}\) and 2P\(_{1/2}\) levels in atomic hydrogen (H) are separated by the famous “1000 Mc/sec” marks a cornerstone of modern physics. Shortly afterwards, Bethe [2] explained the splitting by what is now called the “self-energy” (SE) of the electron. Uehling’s “vacuum polarization” (VP) [3] is too small and has the wrong sign to explain Lamb’s observation.

The initial motivation for a measurement of the Lamb shift in muonic hydrogen (µp, the exotic hydrogen atom made from a proton and a negative muon (µ)) was to study VP [4]. VP does of course also contribute to the Lamb shift in ordinary hydrogen, but in µp, VP is the dominant contribution. This is due to the fact that the mass of the muon is 207 times the mass of the electron, and hence the Bohr orbit in muonic hydrogen is smaller by 207 times the mass of the electron, and hence the Bohr orbit in muonic hydrogen is smaller by what is now called the “self-energy” (SE) of the electron. Uehling’s “vacuum polarization” (VP) [3] is too small and has the wrong sign to explain Lamb’s observation.

In addition, the large reduced mass results in a strong enhancement of the effect of the finite size of the proton on the S levels. The finite size effect depends on the overlap of the muon wave function with the proton charge distribution, and scales with the third power of the reduced mass. The finite size effect on the 2S state in muonic hydrogen is as much as 2% of the total Lamb shift (Fig. 1).

1.1 X-rays from muonic hydrogen

The first X-rays from muonic hydrogen atoms were observed in 1970 [5], and the search for the metastable 2S state began. This state is crucial for Lamb shift measurement where one aims to create µp atoms in the 2S state, drive the 2S–2P transition using a laser pulse around \(H = \mu_p\) and \(\mu_H\) (which corresponds to the 0.2 eV 2S Lamb shift in the center of mass system) should survive on the order of a thousand collisions before undergoing Stark decay (2P–2S mixing during a collision) to the 1S ground state. This results in a 2S quench rate of less than the muon decay rate at gas pressures well below one bar or so [17, 19, 20]. These slow µp(2S) atoms constitute the so-called “long-lived” µp(2S) population. They should be detectable via the Lyman-α X-rays emitted in the Stark decay.

A series of experiments failed to observe these delayed K\(_{\alpha}\) X-rays and (wrongly) concluded that the long-lived µp(2S) population [13–15] is made from the fast µp (1S or 2S) atoms [13–15]. The vast majority of these atoms de-excite to the 1S ground state and are hence of no use for the laser experiment. Furthermore, this de-excitation happens also via emission of Lyman-α, β, γ, ... X-rays (Fig. 2a), and this creates a severe background at “prompt” times, i.e., at the time of µp (1S or 2S) formation. A way out is to fire the laser pulse at “delayed” times, i.e., a few hundred nanoseconds after the prompt muonic cascade is over, to avoid the prompt background. This then defines two crucial requirements for the feasibility of the laser experiment: (i) The µp (2S) population must be “sufficiently high”, i.e., at least about 1% of all muons should form µp (2S) states and (ii) the 2S lifetime should be “sufficiently long”, i.e., the few hundred ns required to avoid the prompt Lyman X-rays.

1.2 Search for the 2S state

The fraction of muons reaching the 2S state during the prompt cascade, \(e_{2S}^{\text{prompt}}\), was deduced between 1977 and 1984 from the measurement of K-line intensity ratios [8–10]: at low H\(_2\) gas pressures, the nP states with \(n \geq 3\) decay mostly radiatively to the 1S ground state or to the 2S metastable state. Therefore, one can calculate the number of µp (2S) atoms by observing the atoms reaching the 1S state, by counting the number of K\(_{\alpha}\), K\(_{\beta}\), K\(_{\gamma}\), etc., X-rays (the so-called “K-line intensities”),

\[
e_{2S}^{\text{total}} = \frac{I_{K_{\alpha}}}{I_{K_{\alpha}}} + \frac{I_{K_{\beta}}}{I_{K_{\alpha}}} + \frac{I_{K_{\gamma}}}{I_{K_{\alpha}}} + \cdots\]

Here, \(I_{K_{\alpha}}\) = \(I_{K_{\beta}}\) + \(I_{K_{\gamma}}\) + \(I_{K_{\gamma}}\) + ⋅⋅⋅ is the total number of K X-rays. The calculated [11] radiative branching ratio 3P→2S/3P→1S is 0.134, and the average branching ratio for \(n \geq 3\) P states is 0.144.

The X-ray measurements [8–10] determined \(e_{2S}^{\text{total}}\) at pressure ranges from a fraction of one mbar up to atmospheric pressure. The value of \(e_{2S}^{\text{total}}\) is as large as 3% at 1 mbar of hydrogen gas pressure (black squares and triangles in Fig. 3).

1.3 2S lifetime

The accepted scenario [17, 18] at that time was that any µp(2S) atom with a kinetic energy (k.e.) below 0.31 eV (which corresponds to the 0.2 eV 2S Lamb shift in the center of mass system) should survive on the order of a thousand collisions before undergoing Stark decay (2P–2S mixing during a collision) to the 1S ground state. This results in a 2S quench rate of less than the muon decay rate at gas pressures well below one bar or so [17, 19, 20]. These slow µp(2S) atoms constitute the so-called “long-lived” µp(2S) population. They should be detectable via the Lyman-α X-rays emitted in the Stark decay.

In vacuum, the µp(2S) lifetime is essentially equal to the muon lifetime. Collisional quenching, like the abovementioned Stark decay, can be reduced by working with sufficiently low gas pressures, below a mbar or so. Therefore, we developed methods like fractional cooling of the muon beam [22] and muon trapping in electric fields [23], which ultimately allowed us to stop muons in 0.06 mbar H\(_2\) gas at room temperature, and in a volume small enough to be illuminated by a laser [24].

We determined the k.e. of µp atoms formed after muon stop in H\(_2\) gas at pressures between 0.06 and 16 mbar [13], and we indeed observed a sizeable amount of µp atoms with k.e. below the 0.31 eV threshold energy, which leads to µp(2S) longevity [6, 7, 18]. We concluded that \(e_{2S}^{\text{long}}\) ≈ 1% (see red open circles in Fig. 3), which was in severe contradiction to the much lower upper limits of \(e_{2S}^{\text{long}}\) given by the above mentioned non-observation of X-rays from Stark decay [8–10, 21].

We could finally resolve this contradiction by the first direct observation of non-radiatively quenched long-lived µp(2S) atoms [13–15]; in a collision, radiationless Coulomb de-excitation takes place either via intermediate molecule formation [25, 26] or without [27]. Either way, the 2S binding energy of 1.9 keV is shared among a formed µp(1S)
atom and one proton of a colliding $H_2$ molecule. We observed [14] the $\mu^p(1S)$ atoms with 0.9 keV k.e., and deduced $2S_{\text{long}} \approx 1\%$ [14, 15], in agreement with our previously extracted values (see full circles in Fig. 3). The Coulombic de-excitation limits the lifetime of the long-lived $2S$ states to about 1 $\mu$s at 1 mbar gas pressure [15].

2. The laser spectroscopy experiment

A long-lived fraction $2S_{\text{long}} \approx 1\%$ and a lifetime $\tau_{2S} \approx 1\mu s$ at 1 mbar are sufficient for a laser experiment [28]. The proposal “R98-03” was accepted at PSI [29] in early 1999, and the development of the setup began [30–34].

The principle of the experiment (Fig. 2) is to stop muons in $H_2$ gas and drive the $2S-2P$ transition with a pulsed laser tunable around $\lambda = 6 \mu m$. Lyman-$\alpha$ X-rays at 1.9 keV, which appear in coincidence with the laser pulse are the signature of a successful $2S-2P$ transition. We have finally observed 6 events per hour on resonance, on top of 1 background event (Figs. 4 and 5), and could measure the $2S_{1/2}F_2$ to $2P_{3/2}F_2$ transition frequency in $\mu$p to be 49 881.88 (76) GHz [38].

2.1 Low energy negative muon beam line

The low-energy muon beam line [39] was designed and built at PSI, Switzerland [40]. An overview is shown in Fig. 6, and the details of the final stages are given in Fig. 7. The novel beamline [41] consists of the “cyclotron trap” (CT), the “muon extraction channel” (MEC), and the 5 T solenoid containing the elements depicted in Fig. 7. The CT acts here as a magnetic bottle made from two 4 T ring coils, with $B = 2$ T in the center of the CT. Negative pions enter the CT tangentially at the rate of $10^8$ sec$^{-1}$ and are moderated in a degrader to bring them onto suitable orbits. About 30% of the pions decay into $\mu^-$, which are further decelerated by repeatedly passing a metallized thin Formvar foil placed in the center of the CT. This foil is kept at $-20$ kV potential. The $\mu^-$ are confined in the magnetic bottle until this repulsive electric field dominates over the magnetic forces. Muons leave the CT close to the axis and enter the MEC, a toroidal momentum filter (magnetic field $B = 0.15$ T), which favors muons with $\sim 20$ keV/c momentum and separates them from background radiation. From the MEC, the muons are guided into the bore hole of a 5 T superconducting magnet, slightly above its axis. The high magnetic field of the solenoid ensures a small radial size of the muon beam, thereby reducing the target volume to be illuminated by the laser. Before entering the hydrogen target,
the muons pass two stacks of ultra-thin carbon foils (area density $d = 4 \, \text{mg/cm}^2$), kept at high electric potential, which both serve as muon detectors and decelerate the muons to 3–6 keV. Each muon releases a few electrons in the stack-foils, which are separated from the much slower muons in an $E/B$ separator field. The electrons are detected by plastic scintillators and photomultiplier tubes and provide the trigger signal for the data acquisition system and the laser.

Finally, the muons arrive in the gas target that is filled with 1.0 mbar of H$_2$ gas and has a length of 20 cm along the beam axis. The transverse dimensions of the stop volume are $5 \, \text{mm} \times 12 \, \text{mm}$. Roughly half of the muons stop inside the volume, which is later illuminated by the laser light.

### 2.2 Laser system for $\lambda = 6 \, \mu\text{m}$

The design of the laser system [42, 43] is dictated by the nature of the muon beam and the lifetime of the 2S state.

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The disk laser technology was one key to the success of the experiment in 2009. The all solid-state design of the laser resulted in nearly 100% up-time over the several weeks of data acquisition. Moreover, pumping the Yb:YAG lasers continuously with up to 1.4 kW of cw pump power ensures a short internal delay of about 250 ns between muon trigger and pulse output from the Yb:YAG oscillators. After SHG, as much as 53 mJ of green pulse energy at $\lambda = 515 \text{ nm}$ is available.

The pulsed TiSa laser consists of an oscillator, providing 1.5 mJ of tunable red light around $\lambda = 708 \text{ nm}$, followed by a multi-pass amplifier, which boosts the pulse energy to 15 mJ. A pulse length of $\sim 5 \text{ ns}$, given by the TiSa oscillator length and some pulse shortening inside the TiSa amplifier, is optimal for subsequent efficient Raman–Stokes conversion in a high-pressure H$_2$ Raman cell [45]. Here, three sequential vibrational Stokes shifts (4155.22(2) cm$^{-1}$) in 15 bar of H$_2$ convert the pump pulses at $\lambda = 708 \text{ nm}$ via 1.0 and 1.7 m$m$ to the desired 6 m$m$ wavelength.

We obtained pulses of 0.25 mJ at 6 m$m$, which we separated from the various other wavelengths (pump light and light from vibrational and rotational Stokes and anti-Stokes of different order) first by a CaF$_2$ prism, and further by a Ge window anti-reflection coated for 6 m$m$ wavelength. The 6 m$m$ infrared (IR) light is easily absorbed by water vapor in air. Therefore, the IR light was sent from the laser hut to the muon beam area through an evacuated tube of $\sim 12 \text{ m}$ length. Before and after the IR light was transported in a dry N$_2$ atmosphere using N$_2$ gas from a LN$_2$ dewar. About 0.1 mJ of the 6 m$m$ light reached the entrance of the target cavity.

The target cavity is depicted in Fig. 9. It was designed to illuminate the elongated muon stop volume (175 mm along the beam axis, 5 mm in height, and about 15 mm in width) from the side. In addition, we wanted to avoid any active mirror stabilization in the H$_2$ target gas and in the 5 T magnetic field. This was accomplished by a robust design using a flat entrance mirror with cylinder pieces attached for the horizontal confinement and an opposing cylindrical mirror for vertical confinement. Injection of the 6 m$m$ light was ensured by an off-axis parabolic mirror that focused the light through a 0.6 mm diameter injection hole in the flat part of the entrance mirror. Off-center injection enabled illumination of a large volume. The final Ge/ZnS HR coating with $R \approx 99.89\%$ reflectivity resulted in an enhancement factor of several hundred. 0.1 mJ of light injected into the cavity did therefore result in a 30% transition probability on the center of the resonance.

Frequency control of the laser system works as follows. The pulsed TiSa oscillator is injection seeded by cw light from a single frequency cw TiSa ring laser. The cw TiSa is at all times locked to a transmission peak of a stable Fabry–Perot (FP) reference cavity with a free spectral range (FSR) of 1497.332(3) MHz.

The pulsed TiSa system follows the laser frequency of the cw TiSa, apart from a measured chirp [42] of about 0.1 GHz. The three sequential Stokes shifts inside the Raman cell remove a constant energy of 3 times the vibrational $n=0$ separation in H$_2$ from each photon. As a consequence, a detuning of the cw TiSa by a frequency $\Delta \nu$ results in the same detuning $\Delta \nu$ of the laser frequency at 6 m$m$.

The laser wavelength at 6 m$m$ is of course well-known from the measured wavelength of the cw TiSa laser and the known Raman shift, with a small correction due to the measured chirp in the pulsed TiSa oscillator and amplifier. However, to minimize systematic uncertainties, we performed the laser frequency calibration directly at $\lambda = 6 \text{ m}$ by means of water vapor absorption in air and in a cell. The absolute position of the water absorption lines have been measured [46] to an absolute precision of 1 MHz, and they are tabulated in the HITRAN database [47]. The total scan range is within less than 100 FSR of the FP, so the 3 kHz uncertainty of the FSR determination by I$_2$, Rb, and Cs spectroscopy is negligible.
The FSR of the FP cavity defines the grid of measurement points of the muonic transition, which has a natural line width of $\Gamma_{25,23} = 18.6$ GHz. The search for the resonance line was performed at every sixth FP fringe, and the final scan of the resonance was done at every other FP fringe (see Fig. 5).

2.3 Detectors for 1.9 keV X-rays

Initially we envisaged gas-scintillation proportional counters (GSPC), read out by CsI-coated micro-strip gas chambers (MSGC) [48], but these were then replaced by large-area avalanche photodiodes (LAAPDs) [49–53]. These have an active surface of 13.5 mm × 13.5 mm, with only very little insensitive surface. They work very well in our strong magnetic field of 5 T [50]. To improve the energy resolution and the signal-to-noise ratio, the LAAPDs are cooled to −30 °C. Their typical time and energy resolutions for 1.9 keV X-rays are 35 ns and 25% (full-width at half maximum), respectively. Ten LAAPDs were mounted above, and 10 below, the muon stop volume inside the target, only 8 mm away from the muon beam center. This resulted in a solid angle coverage of about 20% of 4π. The LAAPDs have been optimized for the detection of the 1.9 keV X-rays from the $\mu p$ (2P→1S) transition, but they are also sensitive to the muon decay electrons. In addition, plastic scintillators have been installed to increase the detection efficiency for decay electrons, whose appearance with some delay following a 2 keV X-ray signal is required in the data analysis to reduce the background. The LAAPD signals are read out using VME waveform digitizers.

Accumulated time spectra on and off resonance are shown in Fig. 4. The laser-induced peak is clearly visible when the laser is tuned to the correct frequency.

3. Results

3.1 The experiment saga

Our first “machine development” beam time took place in 2002. We put together all parts of the experiment and managed to run for a few hours before the end of the beam time. We identified several weak points of the apparatus and changed them before our first real data acquisition run in 2003. The 50 Hz XeCl Excimer laser was replaced by two XeCl Excimer lasers capable of 100 Hz repetition rate. The internal delay of the Excimer lasers could be shortened to 1200 ns. Two parallel dye MOPA systems provided up to 90 mJ of green pump power for the TiSa system. We also replaced the LAAPDs to achieve a larger solid angle and installed a muon-anti-coincidence detector at the end of the gas target to veto laser shots when the muon did not stop inside the gas target.

After three weeks of data acquisition in 2003 the result was very disappointing (Fig. 10). No sign of a resonance could be observed within the “reasonable range” of ±3σ of the prediction using the CODATA value [37] of the proton rms charge radius at FP = 842. We explained the lack of signal with a too long internal delay of the laser system [41]. Now we know better. We spent most of the measurement time around FP = 842, but the peak was finally found in 2009 at FP = 895, at which we had not measured for a long enough time in 2003. In hindsight, of course, one can identify the two right-most points in Fig. 10, which are somewhat higher than the background, with the peak finally observed in 2009.

After the development of the Yb:YAG disk lasers [42, 43], we had another beam time in 2007. Again, we searched for the resonance in the “reasonable” range, but serious technical problems prevented us from taking sufficient data. We seemed to observe an “indication of a signal”, but this was most probably due to background created by the laser system, plasma formation when the tightly focused beam hit the injection hole of the target cavity (Fig. 9). We observed a similar effect in 2009 but could understand the problem and solve it by additional shielding of the X-ray detectors against visible light and by anti-coincidence detectors, which warned us when a plasma was created because of laser misalignment.

The 2007 beam time did however have its successes: We increased the muon rate and decreased the background level, as is apparent from Figs. 10 and 11. The disk laser had a much shorter internal delay than the previously used Excimer lasers. After 1 week of data taking in 2009, again in the “reasonable range” around the CODATA prediction, we had again no sign of a resonance and hence decided to extend the search region. Finally, we found the peak 5σ away from the predicted position using the CODATA rms proton charge radius.

3.2 Lamb shift in muonic hydrogen

The final results of the 1st resonance observed in muonic hydrogen have been published recently [38]. The center of the $2S_{1/2}$ to $2P_{3/2}$ transition in $\mu p$ is at 49 881.88 (76) GHz. The uncertainty of 15 ppm is twice better than our goal presented in the proposal [29]. It consists of 700 MHz statistical uncertainty from the free fit of a Lorentzian resonance line on top of a flat background and the 300 MHz total systematic uncertainty, which is exclusively due to our laser wavelength calibration procedure using water vapor absorption lines. The absolute line position is known to 1 MHz [46, 47], but pulse to pulse instabilities of our laser system limits the frequency determination to 300 MHz uncertainty.
3.3 The charge radius of the proton

The \( 2S_{1/2} \rightarrow 2P_{3/2} \) energy difference \( \Delta \tilde{E} \) in muonic hydrogen is the sum of radiative, recoil, and proton structure contributions, and the fine and hyperfine splittings for our particular transition, and it is given [55–60] by,

\[
\Delta \tilde{E} = 209.9779(49) - 5.2262 r_p^2 + 0.0347 r_p^3 \text{ meV} \tag{1}
\]

where

\[
r_p = \sqrt{\frac{r_p^2}{r_p^2}}
\]

is given in fm. The uncertainty of 0.0049 meV in \( \Delta \tilde{E} \) is dominated by the proton polarizability term [58] of 0.015(4) meV. A detailed derivation of (1) is given in the Supplementary Information of [38].

We deduce a value of the rms charge radius of the proton of

\[
r_p = 0.841 \, 84(36)(56) \text{ fm} \tag{2}
\]

where the first and second uncertainties originate from the experimental uncertainty of 0.76 GHz and the uncertainty in the first term in (1), respectively. Theory, mainly the proton polarizability, gives the dominant contribution to our total relative uncertainty of \( 8 \times 10^{-4} \). Our experimental precision would suffice to deduce \( r_p \) to a relative uncertainty of \( 4 \times 10^{-4} \).

3.4 The proton radius puzzle

This new value of the proton radius \( r_p = 0.841 \, 84(67) \) fm is 10 times more precise, but 5.0\( \sigma \) smaller, than the previous best (CODATA) value \( r_p = 0.876 \, 8(69) \) fm [37], which is mainly obtained from spectroscopy in regular hydrogen (H). It is 26 times more accurate, but 3.1\( \sigma \) smaller, than the previously accepted hydrogen-independent value extracted from electron proton scattering [35, 36] of \( r_p = 0.895(18) \) fm. Furthermore, Bernauer et al. have recently published [61] a more precise charge radius of the proton \( r_p = 0.879(8) \) fm, using new data from the Mainz MAMI electron accelerator. This new electron scattering value agrees with the one obtained from H/D spectroscopy \( r_p = 0.876(8) \) fm (see [37], Table XLV, adjustment 7).

Recent lattice QCD calculations [62], on the other hand, obtain \( r_p = 0.83(3) \) fm, favoring a lower radius than the one from H or electron scattering. Also, dispersion analysis of the nucleon form factors has recently [63] also produced smaller values of \( r_p \in [0.822\cdots0.852] \) fm, in agreement with our accurate value. The situation is summarized in Fig. 12.

3.5 A new value of the Rydberg constant

Assuming for now the correctness of the QED calculations in hydrogen [57, 64] and \( \mu p \) [55, 56, 58–60], we can use our most precise value of \( r_p \) and the most accurately measured transition frequency in hydrogen (1S–2S) [65, 66] to deduce a new value of the Rydberg constant,

\[
R_\infty = 10973 \, 731.568 \, 160(16) \text{ m}^{-1} \tag{3}
\]

This is \( -110 \text{ kHz}/c \) or 4.9\( \sigma \) away from the CODATA value [37], but 4.6 times more precise [1.5 parts in \( 10^{12} \)]. The new determination continues the astonishing improvement in the accuracy of the most accurately determined fundamental physical constant (Fig. 13).

3.6 The charge radius of the deuteron

The precise measurement of the isotope shift of the 1S–2S transition in regular hydrogen and deuterium atoms [67] gives a very accurate value for the difference of the squared charge radii of the proton and the deuteron, \( r_p^2 - r_d^2 = 3.82007(65) \) fm\(^2\). Using this and our precise value of the proton charge radius, we obtain for the rms charge radius of the deuteron,

\[
r_d = 2.12809(31) \text{ fm} \tag{4}
\]

This value is within 0.2\( \sigma \) of the value \( r_d = 2.130(10) \) fm obtained in electron scattering [68], but 27 times more precise. It is 10 times more precise than the CODATA value of \( r_d \), and 3\( \sigma \) away from it.

4. Conclusions and Outlook

The world’s most precise value of the rms proton charge radius \( r_p = 0.841 \, 84(67) \) fm, which we have obtained from laser spectroscopy of the Lamb shift in muonic hydrogen
The Rydberg constant is a cornerstone of the CODATA adjustment of fundamental constants [37]. Its accuracy is now 1.5 parts in $10^{12}$.

Our new value $r_p = 0.841\pm0.012$ fm from $\mu p$ spectroscopy [38] disagrees with the values extracted from hydrogen spectroscopy ([37], Table XLV, adjustment 7), the world average from electron scattering [35, 36], and the new electron scattering value from Mainz [61]. The lattice QCD value is from [62], and the dispersion value is from [63].

$\mu p$, has created a puzzle. The disagreement with the previous values from hydrogen spectroscopy and electron scattering is stunning.

We are confident that the re-evaluation of bound-state QED calculations may soon resolve the puzzle. New insight may also arise from our future project, the measurement of the Lamb shift in the muonic helium ion [69].

Fig. 12. Our new value $r_p = 0.841\pm0.012$ fm from $\mu p$ spectroscopy [38] disagrees with the values extracted from hydrogen spectroscopy ([37], Table XLV, adjustment 7), the world average from electron scattering [35, 36], and the new electron scattering value from Mainz [61]. The lattice QCD value is from [62], and the dispersion value is from [63].

References


